

**POUŽITELNÉ VZORCE PRE PREDMET  
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Rozdelenie	$bin(n, p)$	$hyge(M, K, n)$	$poiss(\lambda)$	$unif(a, b)$	$exp(\lambda)$	$norm(\mu, \sigma)$
E(X)	$np$	$\frac{n \cdot K}{M}$	$\lambda$	$\frac{(a+b)}{2}$	$\lambda$	$\mu$
D(X)	$np \cdot (1-p)$	$\frac{nK(M-K)(M-n)}{M^2(M-1)}$	$\lambda$	$\frac{(a+b)^2}{12}$	$\lambda^2$	$\sigma^2$

$$p(n+1) = p(n) \cdot P; \quad p(n+1) = p(0) \cdot P^{n+1}; \quad a \cdot P = a; \quad Z = [I - (P - A)]^{-1} = I + \sum_{n=1}^{\infty} (P^n - A);$$

$$M = P \cdot (M - \hat{M}) + E; \quad M = (I - Z + E \cdot \hat{Z}) \cdot \hat{M}.$$

$$p(t + \Delta t) = p(t) \cdot P(t, t + \Delta t); \quad p(t + \Delta t) = p(t) \cdot (I + A(t) \cdot \Delta t); \quad F(s) = p(0) \cdot [s \cdot I - A]^{-1}.$$

$$p(t + \Delta t) = p(t) \cdot P; \quad p_0 = 1 - \frac{\lambda}{\mu} = 1 - \rho; \quad P(N > n) = \rho^{n+1}; \quad P(N > 0) = \rho = 1 - p_0; \quad \bar{T} = \frac{\bar{n}}{\lambda};$$

$$\bar{n} = \rho \cdot (1 - \rho) \cdot \sum_{n=1}^{\infty} n \cdot \rho^{n-1}; \quad \bar{n} = \frac{\rho}{1 - \rho} = \frac{\lambda}{\mu - \lambda}; \quad \bar{n}_f = \bar{n} - (1 - p_0) = \frac{\rho^2}{1 - \rho} = \frac{\lambda^2}{\mu \cdot (\mu - \lambda)}; \quad \bar{T}_f = \bar{T} - \frac{1}{\mu};$$

$$p(t + \Delta t) = p(t) \cdot P; \quad p_n = p_0 \cdot \frac{\rho^n}{n!}; \quad p_n = p_0 \cdot \frac{\rho^n}{S^n} \cdot \frac{S^S}{S!}; \quad p_0 = \left[ \sum_{k=0}^{S-1} \frac{\rho^k}{k!} + \frac{\rho^S}{S!} \cdot \frac{1}{1 - \frac{\rho}{S}} \right]^{-1};$$

$$P(N > S) = p_0 \cdot \frac{1}{1 - \frac{\rho}{S}}; \quad \bar{n}_f = \sum_{n=S+1}^{\infty} (n - S) \cdot p_n; \quad \bar{S} = \sum_{n=0}^S (S - n) \cdot p_n; \quad \bar{n} = \bar{n}_f + S - \bar{S};$$

$$\bar{n}_f = p_0 \cdot \frac{\rho^{S+1}}{(S+1)!} \cdot \frac{1}{\left(1 - \frac{\rho}{S}\right)^2}; \quad \bar{T}_f = \frac{\bar{n}_f}{\lambda}; \quad \bar{T} = \frac{\bar{n}}{\lambda} = \bar{T}_f + \frac{1}{\mu}; \quad \bar{S} = S - \rho.$$

$$p_n = \left(\frac{\lambda}{\mu}\right)^n \cdot p_0; \quad p_n = 0; \quad p_0 = \frac{1 - \rho}{1 - \rho^{N+1}}; \quad p_0 = \frac{1}{N+1}; \quad p_n = \frac{(1 - \rho) \cdot \rho^n}{1 - \rho^{N+1}}; \quad p_n = \frac{1}{N+1};$$

$$\bar{n} = \sum_{n=0}^N n \cdot p_n = \frac{\rho \cdot [1 - (N+1) \cdot \rho^N + N \cdot \rho^{N+1}]}{(1 - \rho) \cdot (1 - \rho^{N+1})}; \quad \bar{n} = \sum_{n=0}^N n \cdot p_n = \frac{N}{2}; \quad \bar{n}_f = \bar{n} - \frac{\rho \cdot (1 - \rho^N)}{1 - \rho^{N+1}}; \quad \bar{T} = \frac{\bar{n}}{\lambda^*};$$

$$\bar{T}_f = \frac{\bar{n}_f}{\lambda^*}; \quad \lambda^* = \lambda \cdot (1 - p_N); \quad p_N = \frac{(1 - \rho) \cdot \rho^N}{1 - \rho^{N+1}} = p_0 \cdot \rho^N.$$

$$p_n = \frac{1}{n!} \left( \frac{\lambda}{\mu} \right)^n \cdot p_0 = p_0 \cdot \frac{(S \cdot \rho)^n}{n!}; \quad p_n = \frac{1}{S! \cdot S^{n-S}} \left( \frac{\lambda}{\mu} \right)^n \cdot p_0 = p_0 \cdot \frac{S^S \cdot \rho^n}{S!}; \quad p_0 = \left[ \sum_{n=0}^{S-1} \frac{(S \cdot \rho)^n}{n!} + \sum_{n=S}^N \frac{(S \cdot \rho)^n}{S! \cdot S^{n-S}} \right]^{-1};$$

$$\bar{n}_f = \sum_{n=S}^N (n-S) \cdot p_n = p_0 \cdot \frac{S^S \rho^{S+1}}{S! (1-\rho)^2} \cdot [1 - \rho^{N-S+1} - (1-\rho) \cdot (N-S+1)^{N-S}]; \quad \bar{T}_f = \frac{\bar{n}_f}{\lambda^*}; \quad \bar{T} = \bar{T}_f + \frac{1}{\mu}.$$

$$p_n = p_0 \cdot \rho^n \cdot \frac{M!}{(M-n)!}; \quad p_n = 0; \quad p_0 = \left[ \sum_{n=0}^M \rho^n \cdot \frac{M!}{(M-n)!} \right]^{-1};$$

$$p_n = p_0 \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \binom{M}{n} = p_0 \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \frac{M!}{n! (M-n)!};$$

$$p_n = p_0 \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \binom{M}{n} \cdot \frac{n!}{S! \cdot S^{n-S}} = p_0 \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \frac{M!}{S! \cdot S^{n-S} \cdot (M-n)!}; \quad p_n = 0;$$

$$p_0 = \left[ \sum_{n=0}^{S-1} \binom{M}{n} \cdot \left( \frac{\lambda}{\mu} \right)^n + \sum_{n=S}^M \binom{M}{n} \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \frac{n!}{S! \cdot S^{n-S}} \right]^{-1};$$

$$\bar{n} = p_0 \cdot \left[ \sum_{n=0}^{S-1} n \cdot \binom{M}{n} \cdot \left( \frac{\lambda}{\mu} \right)^n + \sum_{n=S}^M n \cdot \binom{M}{n} \cdot \left( \frac{\lambda}{\mu} \right)^n \cdot \frac{n!}{S! \cdot S^{n-S}} \right];$$

$$\bar{n}_f = \sum_{n=S}^M (n-S) \cdot p_n = \bar{n} - S + p_0 \cdot \sum_{n=0}^{S-1} (S-n) \cdot \binom{M}{n} \cdot \left( \frac{\lambda}{\mu} \right)^n \quad \bar{T} = \frac{\bar{n}}{\lambda \cdot (M - \bar{n})}; \quad \bar{T}_f = \frac{\bar{n}_f}{\lambda^*} = \frac{\bar{n}_f}{\lambda \cdot (M - \bar{n})}.$$

$$p_n = \sum_{m=0}^{n-1} (p_{(n-m),m,1} + p_{m,(n-m),2}) = (1-\rho) \cdot \rho^n; \quad p_0 = 1-\rho; \quad \bar{n}_1 = \frac{\left( \frac{\lambda_1}{\mu} \right) \cdot \left( 1 + \rho - \frac{\lambda_1}{\mu} \right)}{1 - \frac{\lambda_1}{\mu}}; \quad \bar{n}_{f1} = \frac{\rho \cdot \left( \frac{\lambda_1}{\mu} \right)}{1 - \frac{\lambda_1}{\mu}};$$

$$\bar{n}_2 = \frac{\left( \frac{\lambda_2}{\mu} \right) \cdot \left( 1 - \frac{\lambda_1}{\mu} + \rho \frac{\lambda_1}{\mu} \right)}{(1-\rho) \cdot \left( 1 - \frac{\lambda_1}{\mu} \right)}; \quad \bar{n}_{f2} = \frac{\rho \cdot \left( \frac{\lambda_2}{\mu} \right)}{(1-\rho) \cdot \left( 1 - \frac{\lambda_1}{\mu} \right)}; \quad \bar{T}_{f1} = \frac{\lambda}{\mu \cdot (\mu - \lambda_1)}; \quad \bar{T}_{f2} = \frac{\lambda}{(\mu - \lambda) \cdot (\mu - \lambda_1)}.$$